

Sorting Practice – Count sort, Radix sort, Bucket sort

For all sorting algorithms: **Time and Space complexity. Stable? Adaptive? (Data moves)**

Non-comparison sorting

NCS1. (6 points) You are using count sort to sort an array of N numbers, where each number is from the range [0,M]. What is the time complexity (as Theta) of the number of data moves? (For example swapping two records requires 3 data moves.). Briefly justify your answer.

NCS2. (9 points) (Radix sort)

Show how **LSD radix sort** sorts the following numbers in the given representation (base 10). Show the numbers after each complete round of count sort.

Index:	0	1	2	3	4	5	6
Original Array:	513	145	320	235	141	433	2

NCS3. (4 points) What is the operation you do to map/scale values from range [A,B] to range [X,Y]? You can assume that $A < B$ and $X < Y$. (E.g. [47,49] -> [20,30], [5,10] -> [21,23])

NCS4. (5 pts) Assume you want to use bucket sort to sort an array A, that has integers in the range [-100, 350]. (i.e. $A[i] \geq -100$ and $A[i] \leq 350$, for all valid i). You will use 50 buckets. Write the formula to find the index, `bucketIdx`, for the bucket where A[i] should go.

Make sure you indicate any rounding (up or down) if necessary.

NCS5. (6 pts) Fill in the arrays to show the required processing with count sort for the data below.

	0	1	2	3	4	5	6
Original array	C, Alice	B, Jane	A, Jane	F, John	A, Matt	D, Sam	B, Tom

Counts array after part 1 (counts of each key):

Index:	
Counts array:	

Counts array after part 2 (after cumulative sum):

Index:	
Counts array:	

Show the counts array and the copy array after each of the next 2 big steps of count sort as shown in slide 6 (i.e. after a first element is placed in the copy array, and after a second element is placed in the copy array). Create columns as needed in the tables below.

Index:	
Counts array:	
Counts array:	

Index:	
Copy array:	
Copy array:	

NCS6. a) We run bucket sort (version covered in class) on the array [0.3, 0.15, 0.27, 0.8, 0.61].

How many buckets will be created?

What are the elements in each bucket? Here we assume the numbers in the array are in the range [0,1) and we map these to the bucket indexes (like in the pseudocode). We do NOT use the min and max from the array.

When giving the elements in a bucket, give them in SORTED order, separated by commas and with no extra spaces. Say *empty* if the bucket is empty.

b) What if 10 buckets were created?