

CSE-4303 CSE5365 Computer Graphics Practice Perspective Projections

The viewing parameters for the perspective projection are given as

$$\begin{aligned} \text{VRP(WC)} &= (1, 2, 3) & \text{VPN(WC)} &= (3, 4, 5) \\ \text{VUP(WC)} &= (3, 6, 4) & \text{PRP (VRC)} &= (2, 5, 4) \\ u_{\min} \text{ (VRC)} &= 7 & u_{\max} \text{ (VRC)} &= 11 \\ v_{\min} \text{ (VRC)} &= -1 & v_{\max} \text{ (VRC)} &= 1 \\ n_{\min} \text{ (VRC)} &= 6 & n_{\max} \text{ (VRC)} &= 9 \end{aligned}$$

Given all other transformations, find the **Scale** matrix which will transform this viewing volume into a standard perspective volume $x=z, x=-z, y=z, y=-z, z=z_{\min}, z=1$

Matrix #2: Rx

1.000	0.000	0.000	0.000
0.000	0.781	-0.625	0.000
0.000	0.625	0.781	0.000
0.000	0.000	0.000	1.000

Matrix #1: Translate

1.000	0.000	0.000	-1.000
0.000	1.000	0.000	-2.000
0.000	0.000	1.000	-3.000
0.000	0.000	0.000	1.000

Matrix #4: Rz

0.996	0.091	0.000	0.000
-0.091	0.996	0.000	0.000
0.000	0.000	1.000	0.000
0.000	0.000	0.000	1.000

Matrix #3: Ry

0.906	0.000	-0.424	0.000
0.000	1.000	0.000	0.000
0.424	0.000	0.906	0.000
0.000	0.000	0.000	1.000

Matrix #6: Shear

1.000	0.000	1.750	0.000
0.000	1.000	-1.250	0.000
0.000	0.000	1.000	0.000
0.000	0.000	0.000	1.000

Matrix #5: Translate

1.000	0.000	0.000	-2.000
0.000	1.000	0.000	-5.000
0.000	0.000	1.000	-4.000
0.000	0.000	0.000	1.000

Matrix #8: Scale

Matrix #7: scale

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The viewing parameters for the perspective projection are given as

$$\text{VRP(WC)}=(3,4,5)$$

$$\text{VPN(WC)}=(8,6,12)$$

$$\text{VUP(WC)}=(1,2,3)$$

$$\text{PRP (VRC)}=(2,5,5)$$

$$u_{\min}(\text{VRC}) = 6$$

$$u_{\max}(\text{VRC}) = 11$$

$$v_{\min}(\text{VRC}) = -3$$

$$v_{\max}(\text{VRC}) = 5$$

$$n_{\min}(\text{VRC}) = 6$$

$$n_{\max}(\text{VRC}) = 10$$

Given all other transformations, find the **Scale** matrices which will transform this viewing volume into a standard perspective volume

Matrix #2: Rx

1.000	0.000	0.000	0.000
0.000	0.894	-0.447	0.000
0.000	0.447	0.894	0.000
0.000	0.000	0.000	1.000

Matrix #4: Rz

0.417	0.909	0.000	0.000
-0.909	0.417	0.000	0.000
0.000	0.000	1.000	0.000
0.000	0.000	0.000	1.000

Matrix #6: Shear

1.000	0.000	1.300	0.000
0.000	1.000	-0.800	0.000
0.000	0.000	1.000	0.000
0.000	0.000	0.000	1.000

Matrix #8: Scale

Matrix #1: Translate

1.000	0.000	0.000	-3.000
0.000	1.000	0.000	-4.000
0.000	0.000	1.000	-5.000
0.000	0.000	0.000	1.000

Matrix #3: Ry

0.859	0.000	-0.512	0.000
0.000	1.000	0.000	0.000
0.512	0.000	0.859	0.000
0.000	0.000	0.000	1.000

Matrix #5: Translate

1.000	0.000	0.000	-2.000
0.000	1.000	0.000	-5.000
0.000	0.000	1.000	-5.000
0.000	0.000	0.000	1.000

Matrix #7: scale

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1. The viewing parameters for a perspective projection are given as

$$\text{VRP(WC)}=(2,6,3)$$

$$\text{VPN(WC)}=(6,0,0)$$

$$\text{VUP(WC)}=(0,3,4)$$

$$\text{PRP (VRC)}=(3,6,-10)$$

$$u_{\min}(\text{VRC}) = 1$$

$$u_{\max}(\text{VRC}) = 11$$

$$v_{\min}(\text{VRC}) = -1$$

$$v_{\max}(\text{VRC}) = 3$$

$$n_{\min}(\text{VRC}) = 10$$

$$n_{\max}(\text{VRC}) = 40$$

- a. Find the sequence of transformations which will transform this viewing volume into a standard perspective view volume which is bounded by the planes: $x=z$; $x=-z$; $y=z$; $y=-z$; $z=1$ (Complete the blank matrices)
- b. Find the z_{\min} after all transformations are done.

Matrix #2: Rx

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #1: Translate

1	0	0	-2
0	1	0	-6
0	0	1	-3
0	0	0	1

Matrix #4: Rz

Matrix #3: Ry

Matrix #6 Shear

Matrix #5: Translate

1	0	0	-3
0	1	0	-6
0	0	1	10
0	0	0	1

Matrix #8 Scale

Matrix #7 Scale

Zmin=

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The viewing parameters for a perspective projection are given as:

$$\begin{aligned} \text{VRP(WC)} &= (0,0,0) & \text{VPN(WC)} &= (0, 0,1) \\ \text{VUP(WC)} &= (0,1,0) & \text{PRP (VRC)} &= (4,6,8) \end{aligned}$$

$$\begin{aligned} u_{\min}(\text{VRC}) &= -4 & u_{\max}(\text{VRC}) &= 4 \\ v_{\min}(\text{VRC}) &= -5 & v_{\max}(\text{VRC}) &= 5 \\ n_{\min}(\text{VRC}) &= 12 & n_{\max}(\text{VRC}) &= 18 \end{aligned}$$

Find the sequence of transformations which will transform this viewing volume into a unit cube which is bounded by the planes: $x=z$; $x=-z$; $y=z$; $y=-z$; $z=z_{\min}$; $z=1$

- c. Find the **Translation matrix** (Matrix #5)
- d. Find the **Shear matrix** (Matrix #6)
- e. Find the **scale matrices** (Matrix #7 and Matrix #8).
- f. Find the **zmin** after all transformations are done.

Matrix #2: Rx

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #4: Rz

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #6: Shear

Matrix #8: Scale

Matrix #1: Translate

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #3: Ry

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #5: Translate

Matrix #7: Scale

Zmin=

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The viewing parameters for a perspective projection are given as

$$\text{VRP(WC)}=(0,0,0)$$

$$\text{VPN(WC)}=(0,0,1)$$

$$\text{VUP(WC)}=(0,1,0)$$

$$\text{PRP (VRC)}=(4,7,10)$$

$$u_{\min}(\text{VRC}) = 6$$

$$u_{\max}(\text{VRC}) = 11$$

$$v_{\min}(\text{VRC}) = -3$$

$$v_{\max}(\text{VRC}) = 5$$

$$n_{\min}(\text{VRC}) = 12$$

$$n_{\max}(\text{VRC}) = 20$$

Given all other transformations, find the **shear** matrix which will transform this viewing volume into a standard perspective view volume which is bounded by the planes: $x=z$; $x=-z$; $y=z$; $y=-z$; $z=1$

Matrix #2: Rx

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #4: Rz

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #6: Shear

Matrix #8: Scale

0.1	0	0	0
0	0.1	0	0
0	0	0.1	0
0	0	0	1

Matrix #1: Translate

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #3: Ry

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #5: Translate

1	0	0	-4
0	1	0	-7
0	0	1	-10
0	0	0	1

Matrix #7: Scale

4.0	0	0	0
0	2.5	0	0
0	0	1	0
0	0	0	1

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2. The viewing parameters for a perspective projection are given as
 $VRP(WC)=(0,0,0)$ $VPN(WC)=(0,0,1)$
 $VUP(WC)=(0,1,0)$ $PRP(VRC)=(5,12,-5)$

$$\begin{aligned} u_{\min}(VRC) &= -9 & u_{\max}(VRC) &= 11 \\ v_{\min}(VRC) &= -19 & v_{\max}(VRC) &= -15 \\ n_{\min}(VRC) &= -3.5 & n_{\max}(VRC) &= -1 \end{aligned}$$

Find the sequence of transformations which will transform this viewing volume into a standard perspective view volume which is bounded by the planes: $x=z$; $x=-z$; $y=z$; $y=-z$; $z=1$; $z=z_{\min}$

- g. Find the **Shear matrix** (Matrix #6)
h. Find the **scale matrices** (Matrix #7 and Matrix #8).
i. Find the **zmin** after all transformations are done.

Matrix #2: Rx

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #4: Rz

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #6: Shear

Scale2

Matrix #1: Translate

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #3: Ry

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #5: Translate

1	0	0	-5
0	1	0	-12
0	0	1	5
0	0	0	1

Scale1

Zmin=

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The viewing parameters for a perspective projection are given as

$$\text{VRP(WC)}=(\mathbf{0,0,0})$$

$$\text{VPN(WC)}=(\mathbf{0, 1,0})$$

$$\text{VUP(WC)}=(\mathbf{1,0,0})$$

$$\text{PRP (VRC)}=(\mathbf{-2,6,-30})$$

$$u_{\min}(\text{VRC}) = \mathbf{8}$$

$$u_{\max}(\text{VRC}) = \mathbf{18}$$

$$v_{\min}(\text{VRC}) = \mathbf{-9}$$

$$v_{\max}(\text{VRC}) = \mathbf{6}$$

$$n_{\min}(\text{VRC}) = \mathbf{-27}$$

$$n_{\max}(\text{VRC}) = \mathbf{-26}$$

Find the sequence of transformations which will transform this viewing volume into a standard perspective view volume which is bounded by the planes: $x=z$; $x=-z$; $y=z$; $y=-z$; $z=1$; $z=z_{\min}$

- j. Find the **sequence of matrices**
- k. Find the **zmin** after all transformations are done.

Matrix #2: Rx

Matrix #1: Translate

1	0	0	0
0	1	0	0
0	0	1	0
0	0	0	1

Matrix #4: Rz

Matrix #3: Ry

Matrix #6: Shear

Matrix #5: Translate

Scale2

Scale1

Zmin=

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The viewing parameters for a perspective projection are given as

$$\mathbf{VRP}(WC) = (0, 0, 0)$$

$$\mathbf{VPN}(WC) = (0, 0, 2)$$

$$\mathbf{VUP}(WC) = (0, 1, 4)$$

$$\mathbf{PRP}(VRC) = (10, 20, 25)$$

$$u_{\min}(VRC) = 3$$

$$u_{\max}(VRC) = 11$$

$$v_{\min}(VRC) = 6$$

$$v_{\max}(VRC) = 26$$

$$n_{\min}(VRC) = 27$$

$$n_{\max}(VRC) = 30$$

Find the sequence of transformations which will transform this viewing volume into a standard perspective view volume which is bounded by the planes: $x=z$; $x=-z$; $y=z$; $y=-z$; $z=1$

Show the matrices for Problem 1

Matrix #2

Matrix #1

Matrix #4

Matrix #3

Matrix #6

Matrix #5

Matrix #8

Matrix #7
