Your name as it appears on your UTA ID Card

Multiple Choice:

- 1. Write the letter of your answer on the line (_____) to the LEFT of each problem.
- 2. CIRCLED ANSWERS DO NOT COUNT.
- 3. 3 points each
- 1. The maximum number of rotations while inserting a key into a red-black tree is:



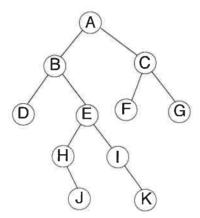
A. 1

B. 2

C. 3

D. the black-height

2. Suppose the tree below is a binary search tree whose keys and subtree sizes <u>are not shown</u>. Which node will contain the key with rank 6? (Write the node's letter on the line.)



I

3. For which of the following sorts does the decision tree model not apply?



A. Insertion

B. LSD Radix Sort

C. MERGE-SORT

D. QUICKSORT

4. In the example of recycling the elements of a list in O(1) time, which situation holds?



- A. Both lists are circular
- B. Both lists are not circular
- C. The list to be recycled is circular, the garbage list is not
- D. The garbage list is circular, the list to be recycled is not
- 5. Given a pointer to a node, the worst-case time to delete the node from a singly-linked list with *n* nodes in ascending order is:



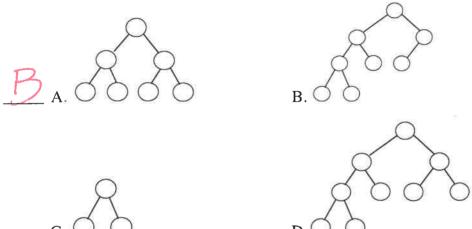
A. Θ(1)

B. $\Theta(\log n)$

C. $\Theta(n \log n)$

D. $\Theta(n)$

~ *	ose that only numbers in 1 100 app hich of the following sequences of key	pear as keys in a binary search tree. While searching for vs could not be examined?	,
A	A. 10, 40, 70, 30, 50 C. 10, 30, 70, 60, 50	B. 1, 100, 20, 70, 50 D. 100, 20, 80, 30, 50	
7. Which	of the following binary trees has exac	etly one legal coloring as a red-black tree?	



8. What does counting sort count?



- A. the number of bytes in the input array
- B. the number of occurences for each possible key value
- C. the number of different input values that have occured
- D. the maximum length among all the strings being sorted
- The subset sum problem takes n input values and attempts to find a combination of those values whose sum is m. The worst-case time to extract the solution from the dynamic programming table is:



- A. $\Theta(\log m)$ B. $\Theta(n)$
- C. $\Theta(m)$
- D. $\Theta(mn)$
- 10. Which of the following will not be true regarding the decision tree for HEAP-SORT for sorting n input values?



- A. There will be n! leaves.
- B. Every path from the root to a leaf will have $O(n \log n)$ decisions.
- C. The height of the tree is $\Omega(n \log n)$.
- D. There will be a path from the root to a leaf with $\Omega(n^2)$ decisions.
- 11. Suppose a node x in an unbalanced binary search tree has two children, each storing one key. What is the first step to delete x?



- A. Find the successor of x
- B. Inorder traversal
- C. Rotate x so it becomes a leaf
- D. Splice the parent of x to either child of x

12. If POP is implemented as return stack[SP--], then PUSH of element X is implemented as:



- A. return stack[SP++] B. stack[SP++] = XC. stack[--SP] = X D. stack[++SP] = X

13. Suppose a (singly) linked list is used to implement a queue. Which of the following is true?



- A. Like a circular queue, the maximum number of items is determined at initialization.
- B. The head points to the first element and the tail points to the last element.
- C. The tail points to the first element and the head points to the last element.
- D. One node is always wasted.
- 14. Which binary tree traversal corresponds to the following recursive code?

```
void traverse(noderef x)
if (x==null)
 return:
traverse(x.left);
traverse(x.right);
// process x here
```



A. inorder B. postorder C. preorder D. search for key x

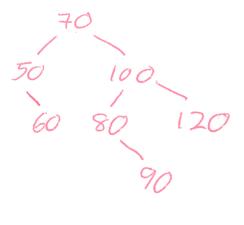
15. The purpose of the binary searches used when solving the longest (monotone) increasing subsequence (LIS) problem is:



- A. to sort the original input
 - B. to assure that the final solution is free of duplicate values
 - C. to determine the longest possible increasing subsequence terminated by a particular input value
 - D. to search a table that will contain only the LIS elements at termination

Long Answer

1. Give the unbalanced binary search tree that results when the keys 70, 50, 100, 80, 60, 90, 120 are inserted, in the given order, into an initially empty tree. (5 points)



```
5 12
1 2 3 4 8
i S
       0
                   0
1
2
3
4
8
C
       1
2
3
4
       5
i
       0
1
2
3
4
5
6
7
                   0
1
2
2
3
3
3
4
4
4
4
      8
   9
10
   11
12
                   5
5
Solution
i S
      5
                  8
3
1
      3
1
```

2. Use the dynamic programming solution for subset sums to determine a subset that sums to 12. (10 points)

AB	8		2		3		1		9		0		7		6		4		5	
Α	8	В	2		3		1		9		0		7		6		4		5	
	2	Α	8	В	3		1		9		0		7		6		4		5	
	2		3	Α	8	В	1		9		0		7		6		4		5	
	2		3		1	Α	8	В	9		0		7		6		4		5	
	2		3		1	Α	8		9	В	0		7		6		4		5	
	2		3		1		0	Α	9		8	В	7		6		4		5	
	2		3		1		0	Α	9		8		7	В	6		4		5	
	2		3		1		0	Α	9		8		7		6	В	4		5	
	2		3		1		0		4	Α	8		7		6		9	В	5	
	2		3		1		0		4	<	5	>	7		6		9		8	

de .

3. Show the result after Partition (Version 1) manipulates the following su pointers start at the left end of the subarray. (10 points)	barray. Recall that both
---	--------------------------

8 2 3 1 9 0 7 6 4 5

100101 011010

LCS is 1010, length==4

0 1 1 0 1 0

0 0 0 0 0 0

1 0 0 1 1 1 1 1

0 0 1 1 1 2 2 2

0 0 1 1 1 2 2 3

1 0 1 2 2 2 3 3

0 0 1 2 2 3 3 4

1 0 1 2 3 3 4 4

4.	Complete the following example of the efficient dynamic programming technique for finding a
	longest common subsequence. Be sure to provide the backtrace for your LCS using arrows in the
	matrix. (10 points)

1 0 0 1 0 1 0 1 1 0 1 0

0 1 1 0 1 0

0 0 0 0 0 0 0

 $1 \quad 0 \quad 0 \quad 1 \quad 1 \quad 1 \quad 1 \quad 1$

0 0 1 1 1 2 2 2

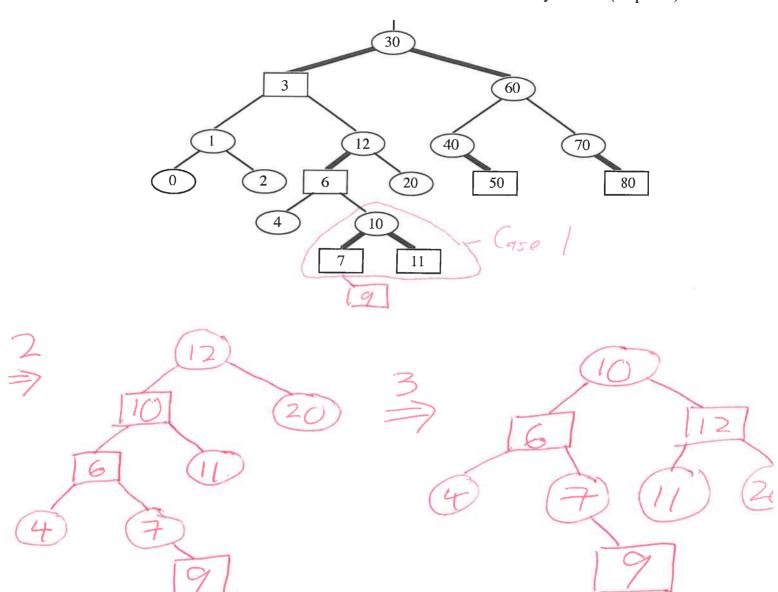
0 0

1 0

0 0

1 0

5. Insert 9 into the given red-black tree. Be sure to indicate the cases that you used (10 points)



6. A billion integers in the range $0...2^{32}$ - 1 will be sorted by LSD radix sort. How much faster is this done using radix $0...2^{8}$ - 1 rather than $0...2^{2}$ - 1? Show your work. (10 points)

$$K = 2^8 = 256$$

$$d = 4$$

$$\Theta(d(n+k))$$

$$\Theta(4(1B+256))$$

$$A$$

$$A = 4$$

$$G(aster)$$

K = 24 = 4 d = 16 3(6(18 + 4)