## CSE 5319/6319 Homework 3

Due April 3, 5:00 p.m. on Canvas

1. Show that the following instance of stable marriages has two stable matchings:

| $\underline{\mathrm{A}}$ | $\underline{\mathrm{B}}$ | $\underline{\mathrm{C}}$ | $\underline{\mathrm{D}}$ | $\underline{\mathrm{E}}$ | $\underline{1}$ | $\underline{2}$ | $\underline{3}$ | $\underline{4}$ | $\underline{5}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 5 | 2 | 3 | 3 | 3 | A | E | A | B | B |
| 1 | 3 | 5 | 2 | 1 | D | B | B | D | E |
| 3 | 5 | 4 | 4 | 2 | C | A | C | A | C |
| 4 | 4 | 1 | 5 | 4 | B | C | E | E | A |
| 2 | 1 | 2 | 1 | 5 | E | D | D | C | D |

2. Find as many maximum-cardinality, pareto-optimal solutions as you can for the following instance of house allocation:

A1: H4 H5 H2 H1 H3
A2: H2 H5 H4 H3 H1
A3: H1 H4 H2 H3 H5
A4: H4 H2 H1 H5 H3
A5: H3 H2 H4 H1 H5
3. A man dies, leaving an estate worth $\$ 600$. The deceased has three widows with marriage contracts of $\$ 150, \$ 250$, and $\$ 350$. Divide the estate among the widows, using the Rule of Linked Vessels.
4. Solve problem 3 using the O'Neill's law/race-to-the-bank method (Shapley Value).
5. A man dies, leaving an estate worth $\$ 250$. The deceased has three widows with marriage contracts of $\$ 50, \$ 100$, and $\$ 200$. Divide the estate among the widows, using the Rule of Linked Vessels.
6. Solve problem 5 using the O'Neill's law/race-to-the-bank method (Shapley Value).

