CSE 5319/6319 Homework 3

Due April 3, 5:00 p.m. on Canvas

1. Show that the following instance of stable marriages has two stable matchings:

<u>A</u>	<u>B</u>	<u>C</u>	<u>D</u>	<u>E</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	<u>5</u>
5	2	3	3	3	А	E	А	В	В
1	3	5	2	1	D	В	В	D	E
3	5	4	4	2	С	А	С	А	С
4	4	1	5	4	В	С	E	E	А
2	1	2	1	5	E	D	D	С	D

- 2. Find as many maximum-cardinality, pareto-optimal solutions as you can for the following instance of house allocation:
 - A1:
 H4
 H5
 H2
 H1
 H3

 A2:
 H2
 H5
 H4
 H3
 H1

 A3:
 H1
 H4
 H2
 H3
 H5

 A4:
 H4
 H2
 H1
 H5
 H3

 A5:
 H3
 H2
 H4
 H1
 H5
- 3. A man dies, leaving an estate worth \$600. The deceased has three widows with marriage contracts of \$150, \$250, and \$350. Divide the estate among the widows, using the Rule of Linked Vessels.
- 4. Solve problem 3 using the O'Neill's law/race-to-the-bank method (Shapley Value).
- 5. A man dies, leaving an estate worth \$250. The deceased has three widows with marriage contracts of \$50, \$100, and \$200. Divide the estate among the widows, using the Rule of Linked Vessels.
- 6. Solve problem 5 using the O'Neill's law/race-to-the-bank method (Shapley Value).